

# Alıştırmalar VI, SOS 129 (2016-17 Güz)

Özer Öztürk

1. Aşağıda verilen işlemlerin sonuçlarını hesaplayın: (b)

(a)

$$\begin{bmatrix} 2 & -1 \\ 3 & 4 \end{bmatrix} + \begin{bmatrix} 3 & 1 \\ 2 & 1 \end{bmatrix}$$

(b)

$$\begin{bmatrix} 2 & -1 \\ 3 & 4 \end{bmatrix} \cdot \begin{bmatrix} 3 & 1 \\ 2 & 1 \end{bmatrix}$$

(c)

$$\begin{aligned} 3z &= 9 \\ x + 5y - z &= 2 \\ x + 6y + z &= 12 \\ x + y + z &= 9 \\ 2x + 4y - z &= 1 \\ 3x + 6y - 5z &= 0 \end{aligned}$$

2. Aşağıda verilen matrislerin  $\mathbb{R}^2$  üzerindeki etkilerini geometrik olarak tarif edin:

(a)

$$\begin{bmatrix} 2 & 0 \\ 0 & -3 \end{bmatrix}$$

(b)

$$\begin{bmatrix} 1 & 1 \\ 1 & 0 \end{bmatrix}$$

(c)

$$\begin{bmatrix} 0 & 1 \\ 1 & 1 \end{bmatrix}$$

(d)

$$\begin{bmatrix} \sqrt{2}/2 & -\sqrt{2}/2 \\ \sqrt{2}/2 & \sqrt{2}/2 \end{bmatrix}$$

(e)

$$\begin{bmatrix} 1 & 1 \\ 1 & 0 \end{bmatrix} \cdot \begin{bmatrix} \sqrt{2}/2 & -\sqrt{2}/2 \\ \sqrt{2}/2 & \sqrt{2}/2 \end{bmatrix}$$

(a)

$$\begin{bmatrix} \sqrt{2}/2 & -\sqrt{2}/2 \\ \sqrt{2}/2 & \sqrt{2}/2 \end{bmatrix}$$

(b)

$$\begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 0 \\ 1 & 0 & 0 \end{bmatrix}$$

(c)

$$\begin{bmatrix} 2 & 1 & 4 \\ 5 & 2 & 3 \\ 8 & 7 & 3 \end{bmatrix}$$

(d)

$$\begin{bmatrix} 1 & 0 & 2 \\ 1 & 3 & 4 \\ 0 & 6 & 0 \end{bmatrix}$$

3. Aşağıda verilen  $\mathbb{R}^2 \rightarrow \mathbb{R}^2$  lineer dönüşümlerine (e) karşılık gelen birer matris bulun:

(a)  $L(x, y) = (2x, -3y)$

(b)  $T(x, y) = (x + y, y)$

(c)  $A(x, y) = (2x + y, -x + 2y)$

(d)  $K(x, y) = (\sqrt{3}x/2 - y/2, x/2 + \sqrt{3}y/2)$

$$\begin{bmatrix} 8 & -1 & 9 \\ 3 & 1 & 8 \\ 11 & 0 & 17 \end{bmatrix}$$

5. Aşağıdaki denklem sistemini çözün:

$$\begin{bmatrix} 8 & -1 & 9 \\ 3 & 1 & 8 \\ 11 & 0 & 17 \end{bmatrix} \cdot \begin{bmatrix} z \\ y \\ x \end{bmatrix} = \begin{bmatrix} 16 \\ 15 \\ 39 \end{bmatrix}$$

4. Aşağıda verilen denklem sistemlerini matris biçiminde yazıp çözün:

(a)

$$2x + y + 3z = 44$$

$$x + y + z = 21$$

$$x + 3y + 2z = 44$$

6. Türkçeye çevirin:

"I would say, if you like, that the party is like an out-moded mathematics...that is to say, the mathematics of Euclid. We need to invent a non-Euclidian mathematics with respect to political discipline."